

# The art of Stokes inversions

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# Outline

- What is an inversion technique?
- How do they work?
- ME inversions
- Accounting for asymmetric Stokes profiles
- Be careful with the choice of model atmosphere!
- Available codes
- Tips and tricks
- Stray-light considerations
- Running SIR
  - Input files
  - Visualization of results

# What is an inversion technique?

- Any method used to infer the physical conditions of the atmosphere from the interpretation of Stokes profiles
  - Center-of-gravity method, bisector analyses, ...
  - Forward modeling
  - PCA, artificial neural networks
  - Least-squares fitting
- What to expect: a model atmosphere capable of reproducing the observations.... **nothing else!**

# Radiative transfer

- The Stokes parameters obey the RTE

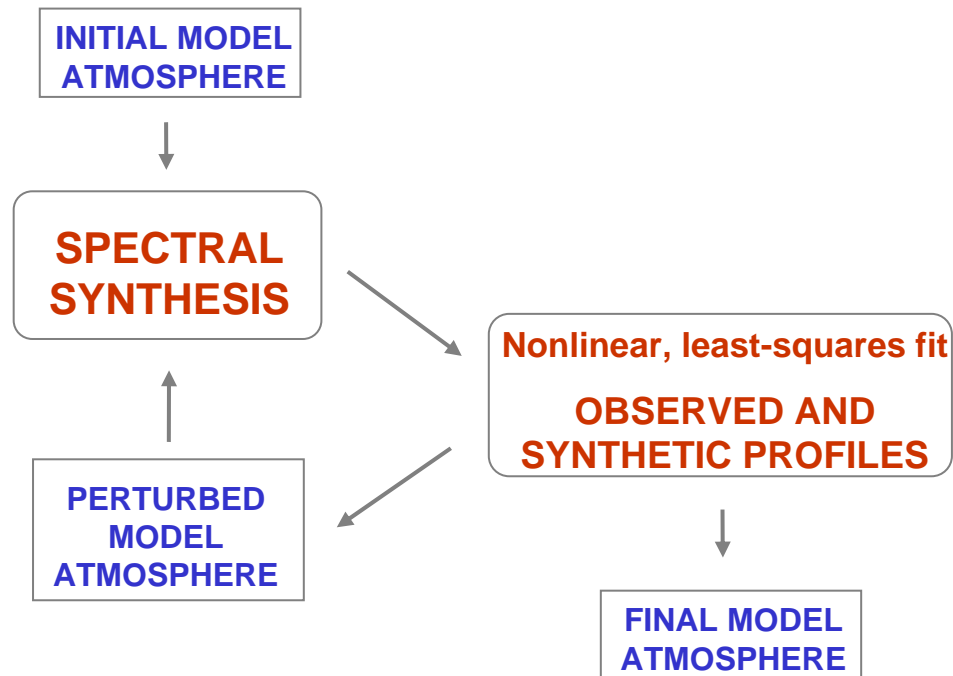
$$\frac{d}{d\tau} \begin{pmatrix} I \\ Q \\ U \\ V \end{pmatrix} = \begin{pmatrix} \eta_I & \eta_Q & \eta_U & \eta_V \\ \eta_Q & \eta_I & \rho_V & -\rho_U \\ \eta_U & -\rho_V & \eta_I & \rho_Q \\ \eta_V & \rho_U & -\rho_Q & \eta_I \end{pmatrix} \begin{pmatrix} I - S \\ Q \\ U \\ V \end{pmatrix}$$

(Unno 1956;  
Rachkovsky 1962)

- $\eta_{I,Q,U,V}$  and  $\rho_{Q,U,V}$  depend on  $\mathbf{a} \equiv (B, \gamma, \chi, v_{\text{LOS}}, T, P_e, v_{\text{mic}})$
- This means that
  - Four Stokes parameters needed to understand just one of them
  - Proper interpretations of the Stokes vector require a good knowledge of the atmosphere ( $\mathbf{a}$ )

# Least-square inversions

- The complete line transfer problem has to be solved
- Self-consistent inferences → Inversion techniques



## Advantages:

- No simplifying assumptions
- Full Stokes vector fitted
- Complex model atmospheres
- All atmospheric parameters inferred at the same time

# How do they work?

- Inversion driven by  $\chi^2$ -minimization:

$$\chi^2(\mathbf{a}) = \sum [I_{obs}(\lambda_i) - I_{syn}(\lambda_i, \mathbf{a})]^2$$

- Linearization: Levenberg-Marquardt algorithm

$$\nabla \chi^2(\mathbf{a}) + \mathbf{A}(\chi^2) \cdot \delta \mathbf{a} = 0$$

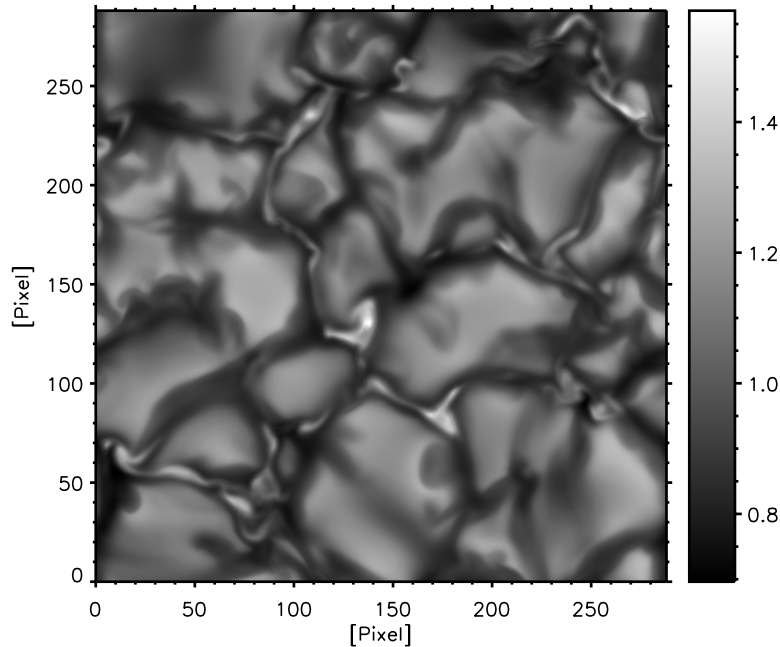
- Keeping the number of free parameters small:
  - Atmospheric parameters perturbed in coarse grid
  - Full stratifications in finer grid by cubic spline interpolation
- Regularization techniques (*when in doubt, smooth*)
  - Penalty function, or
  - Modified SVD method (Ruiz Cobo & del Toro Iniesta 1992)

# Inversions based on ME atmospheres

- ME atmosphere:
  - Source function is linear with optical depth
  - Absorption matrix does not vary with optical depth
- Analytical Stokes profiles
- Fast inversion
- Smooth maps of physical quantities
- Results are relatively accurate and easy to interpret

# ME inversions of high spatial resolution profiles

MHD simulations (Vögler et al. 2005)

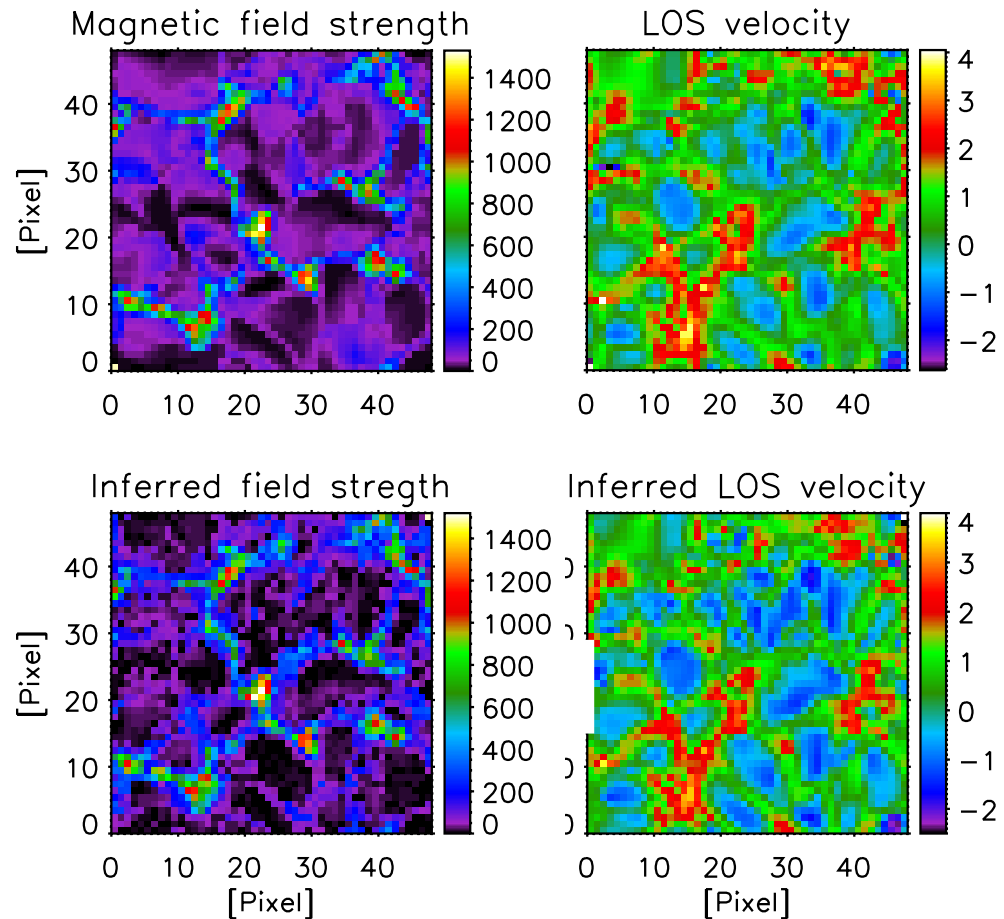
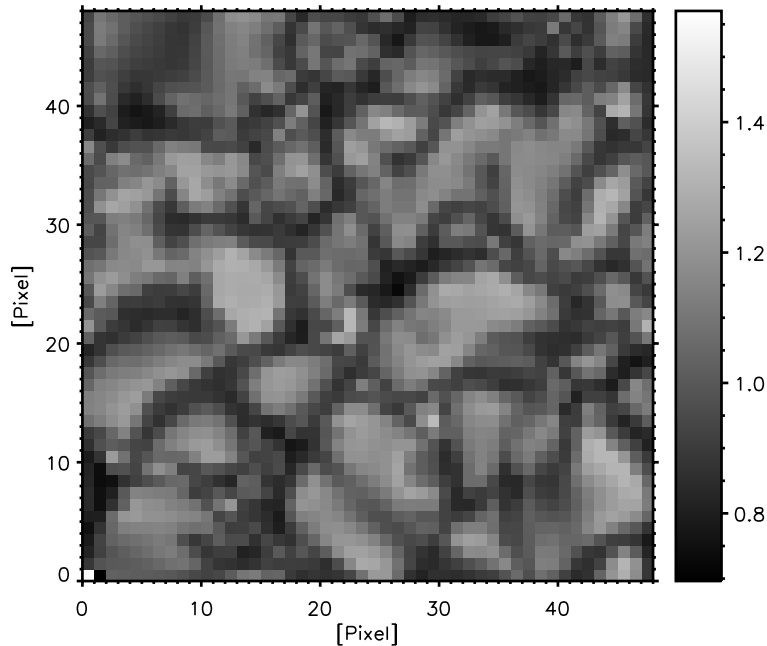


- Fe I 630.1 and 630.2 nm profiles degraded to HINODE/SP pixel size



# ME inversions of high spatial resolution profiles

MHD simulations (Vögler et al. 2005)



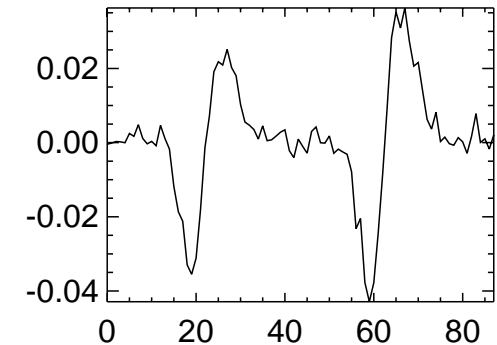
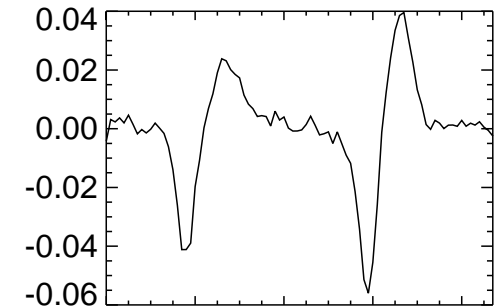
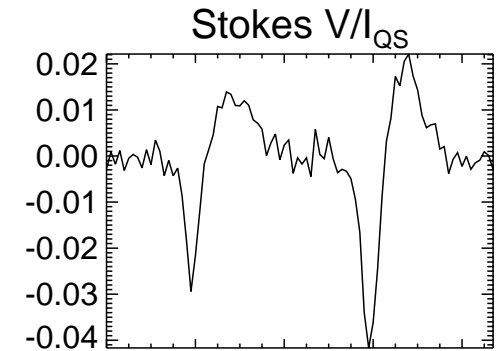
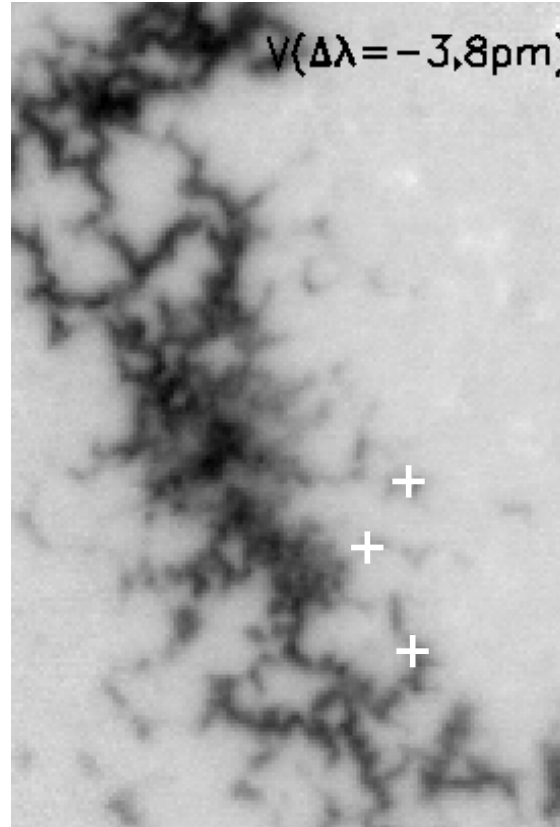
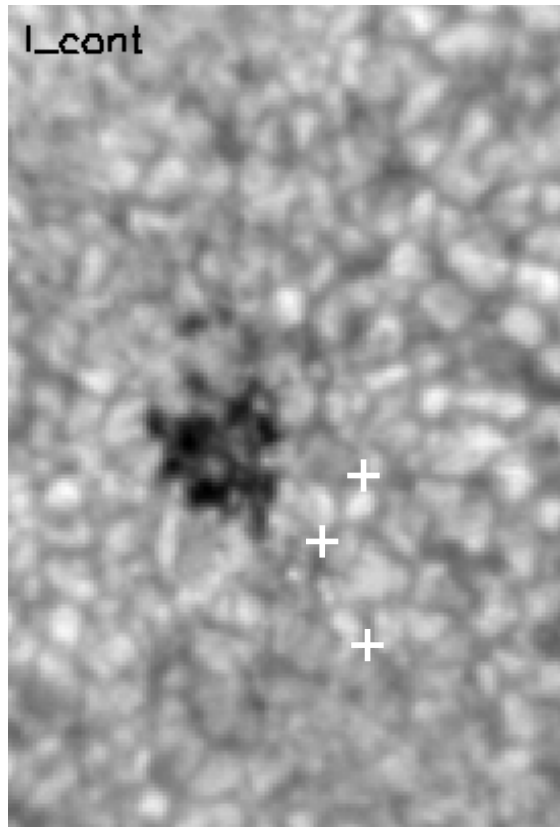
- Fe I 630.1 and 630.2 nm profiles degraded to HINODE/SP pixel size
- Maps of inferred  $B$  and  $v_{\text{Los}}$  very similar to real ones!

Orozco Suárez et al. 2007, ApJL

# Inversions based on ME atmospheres

- ME atmosphere:
    - Source function is linear with optical depth
    - Absorption matrix does not vary with optical depth
  - Analytical Stokes profiles
  - Fast inversion
  - Smooth maps of physical quantities
  - Results are easy to interpret
- 
- Simplistic treatment of radiation transfer
  - Little thermal information. No height variations
  - Cannot account for **asymmetric Stokes profiles**

# Asymmetric Stokes profiles

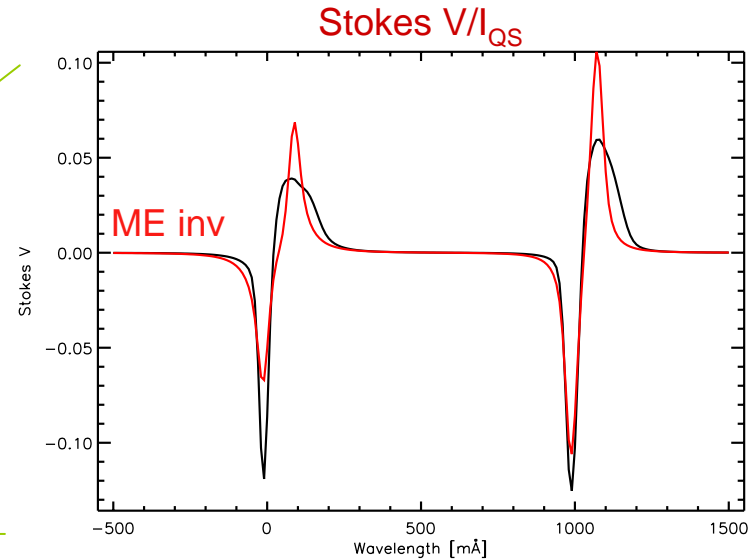
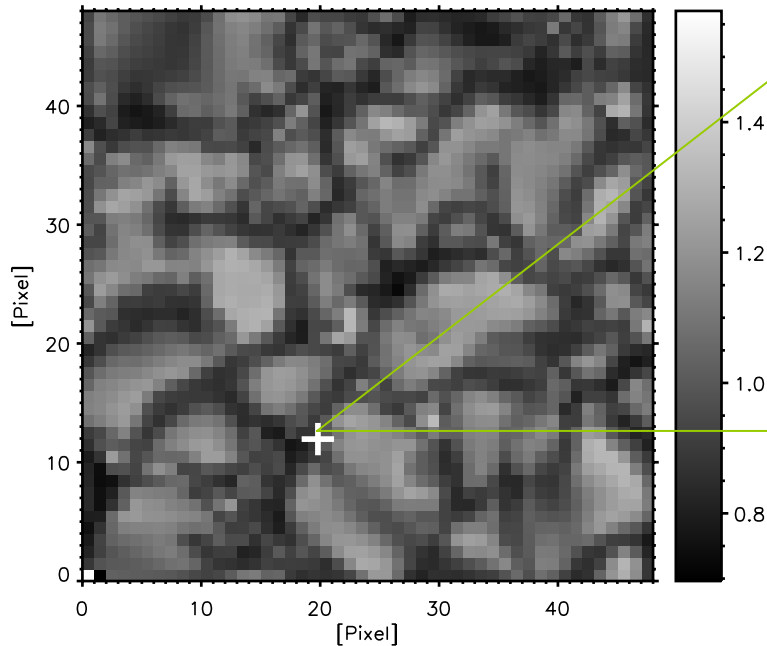


- KIS/IAA Visible Imaging Polarimeter + TESOS + KAOS
- VTT, Observatorio del Teide
- **Spatial resolution:  $\sim 0.4''$**
- Pore near disk center, Fe I 630.15 and 630.25 nm

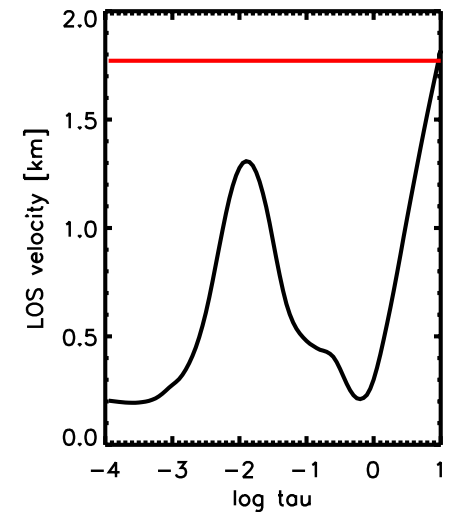
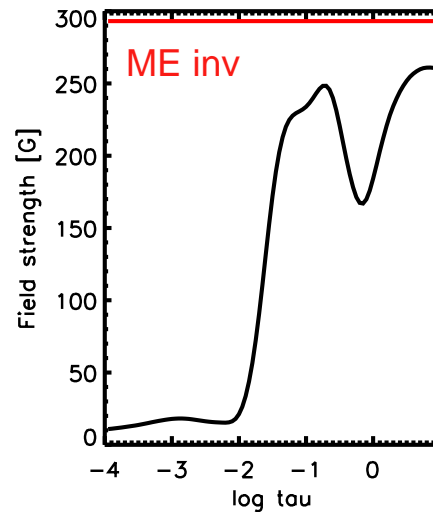
Bellot Rubio et al. (2007)

# ME inversions of asymmetric profiles

MHD simulations (Vögler et al. 2005)



- Stokes profiles not well fitted
- ME results are some kind of “average” of physical parameters along the LOS



# The origin of asymmetries

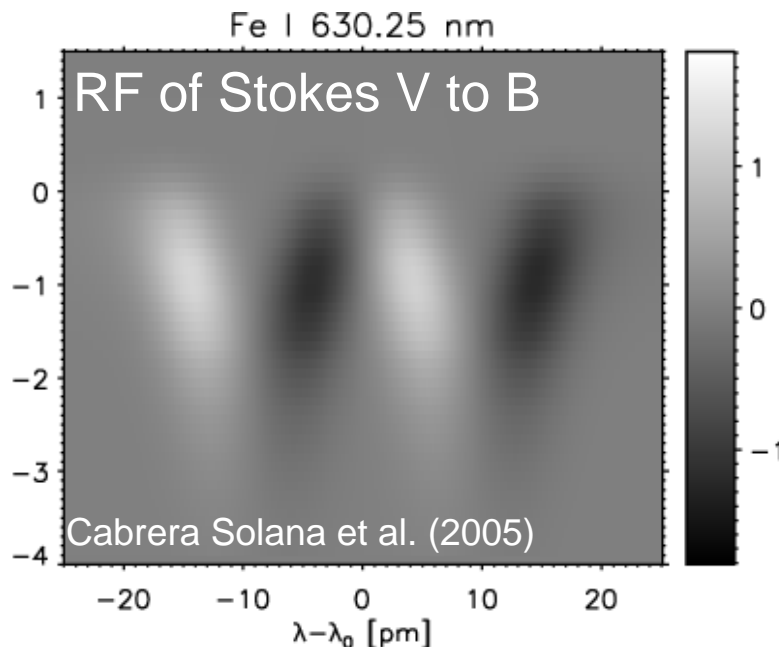
Amplitude asymmetry/  
Multi-lobed Stokes profiles

Different magnetic atmospheres  
coexisting in resolution element

Area asymmetry

Gradients/discontinuities of  
physical parameters along LOS

Auer & Heasley (1978)

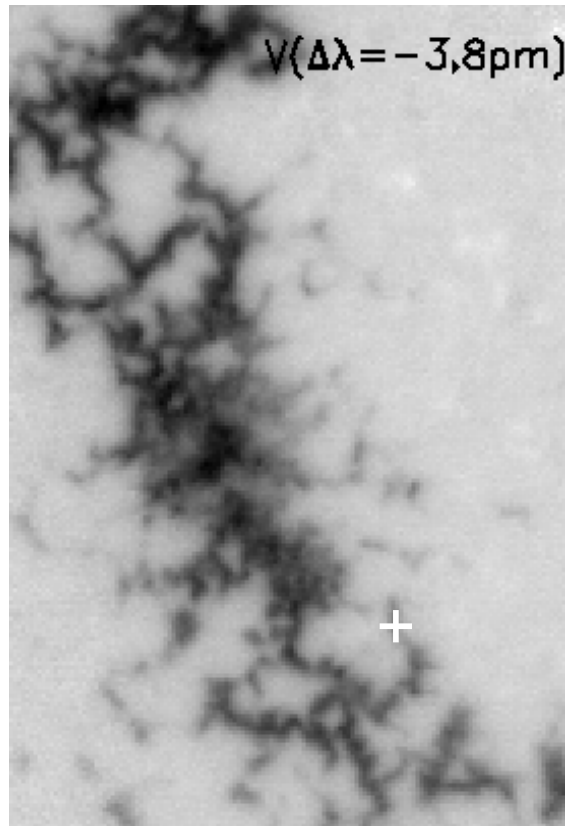


The area asymmetry gives  
information on the height variation  
of atmospheric parameters

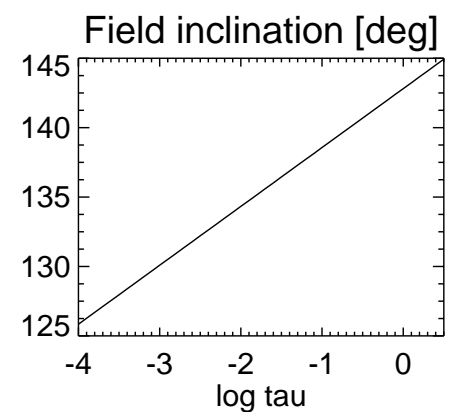
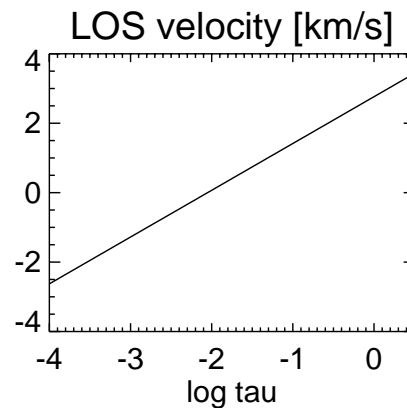
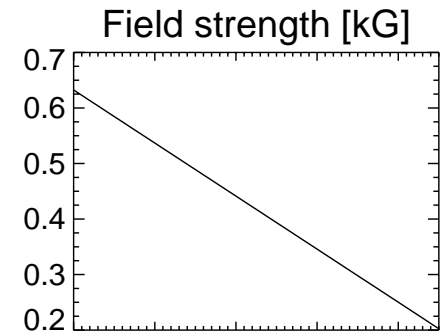
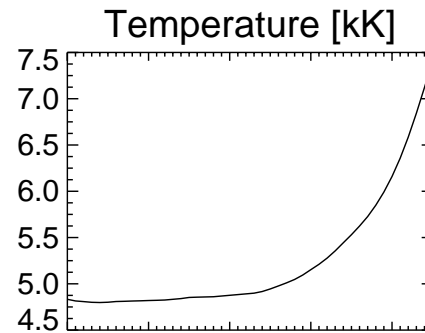
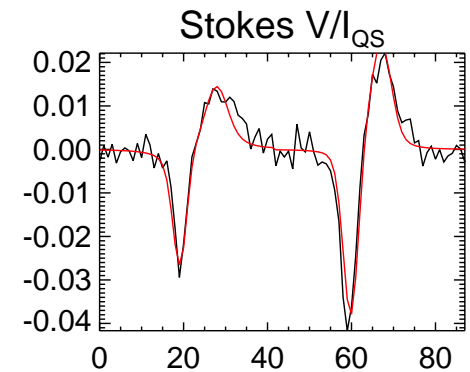
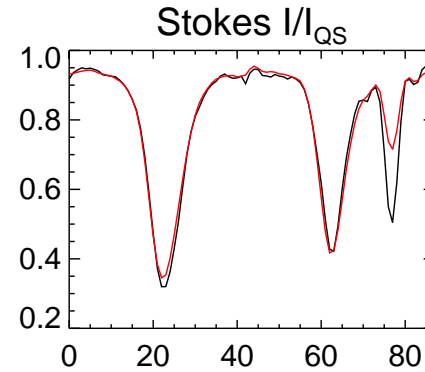
# Accounting for asymmetries

- Inversion codes capable of dealing with asymmetries
  - Are based on numerical solution of RTE
  - Provide reliable thermal information
  - Use *less free parameters than ME* codes
  - Infer stratifications of physical parameters with depth

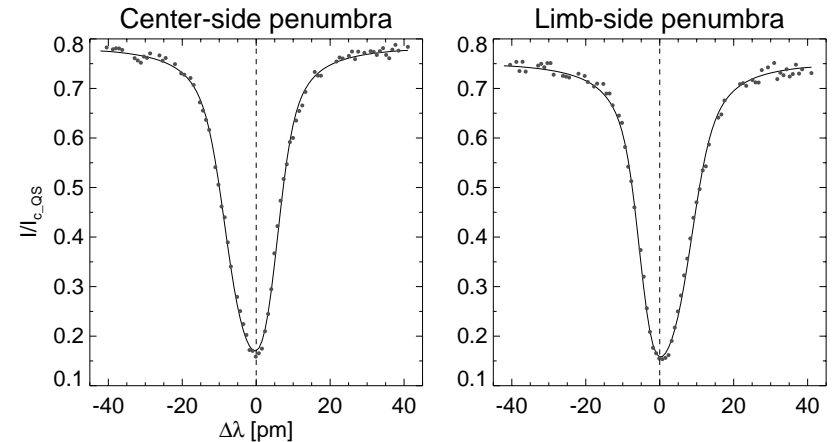
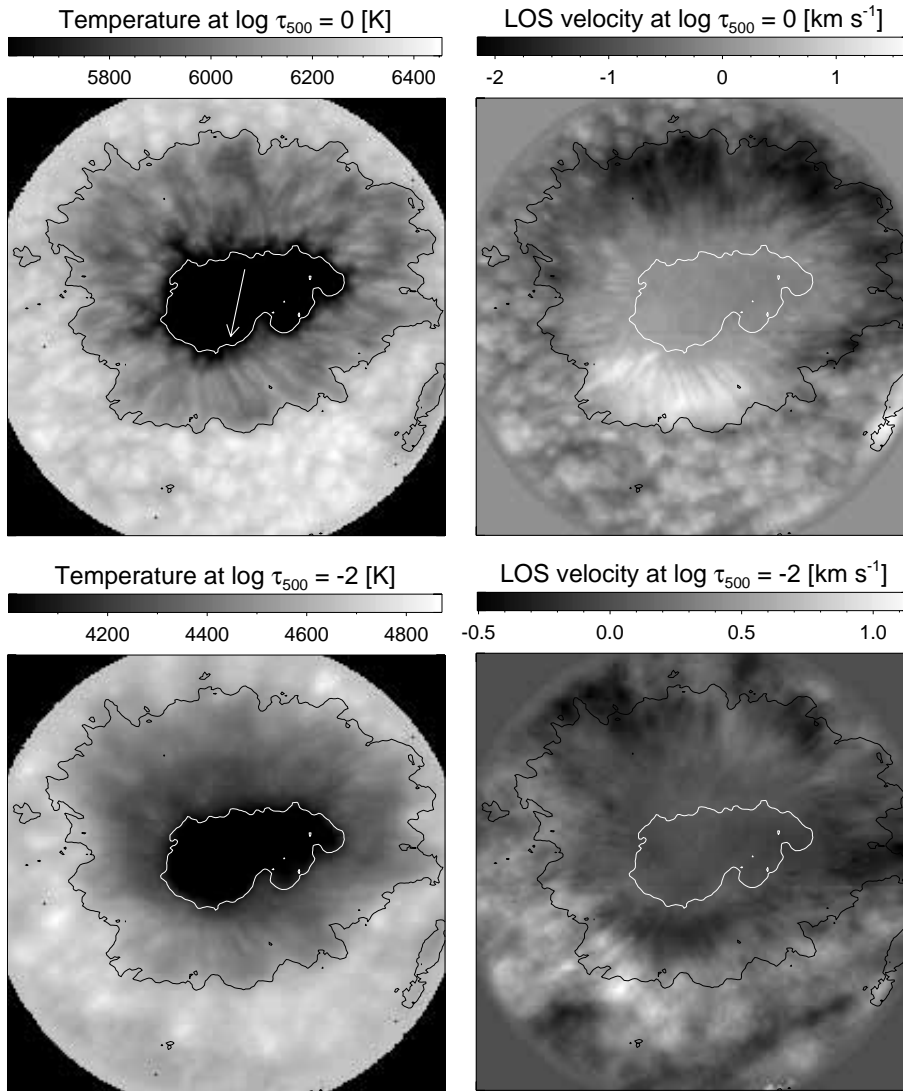
# Accounting for asymmetries



- VIP + TESOS + KAOS
- SIR with 10 free parameters
- Bellot Rubio et al. (2007)



# Inversions with gradients



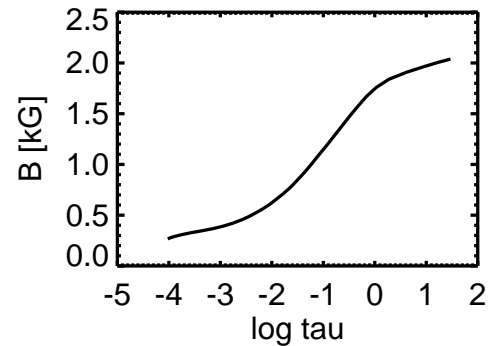
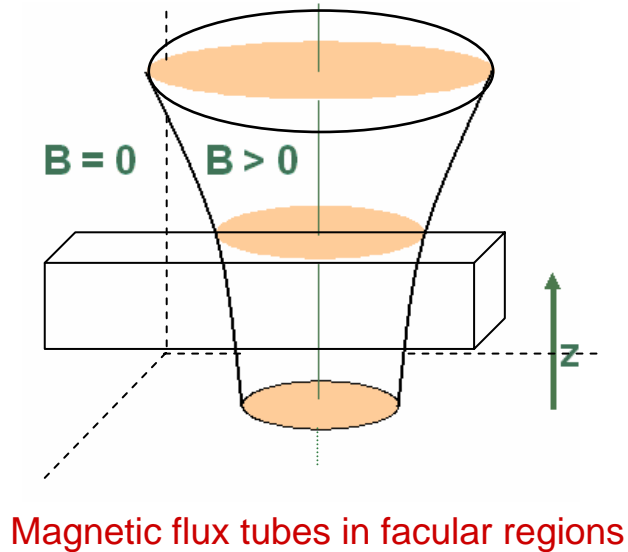
- Spatial resolution  $\sim 0.5''$
- Intensity profiles of Fe I 557.6 nm
- **SIR with 7 free parameters**
- Thermal/kinematic structure of AR 0019 at different heights in the photosphere

Bellot Rubio, Schlichenmaier, & Tritschler 2006, A&A 453, 1117

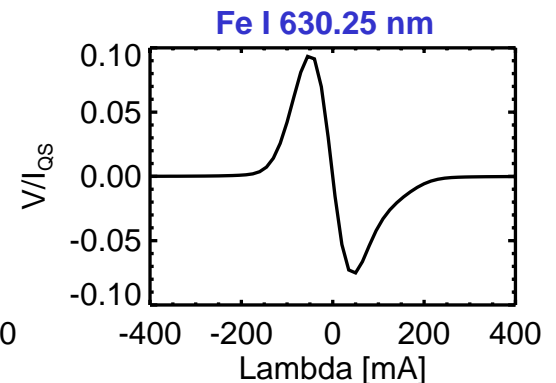
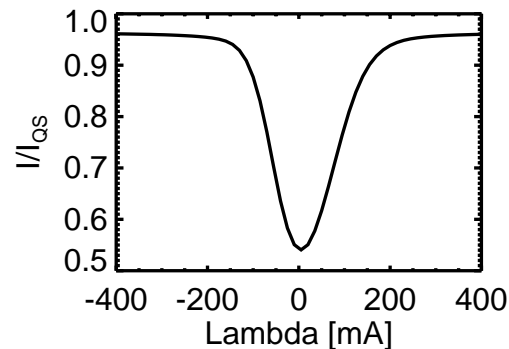


# Be careful with the atmospheric model!

Inversion results change if the physical model is changed  
Models are often simplistic and do not describe the real atmosphere

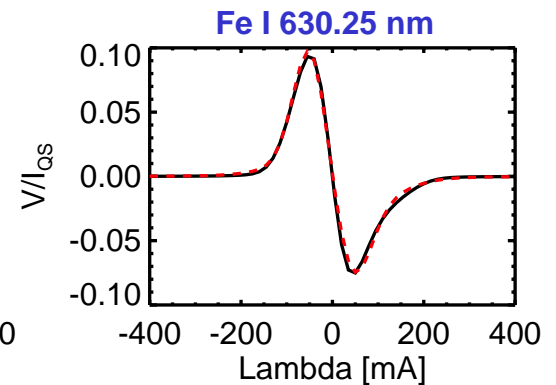
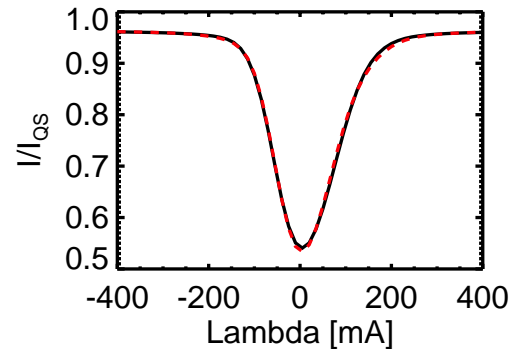
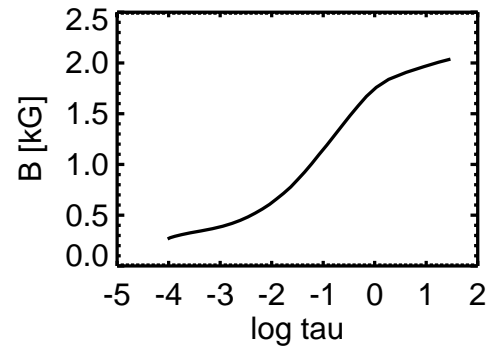
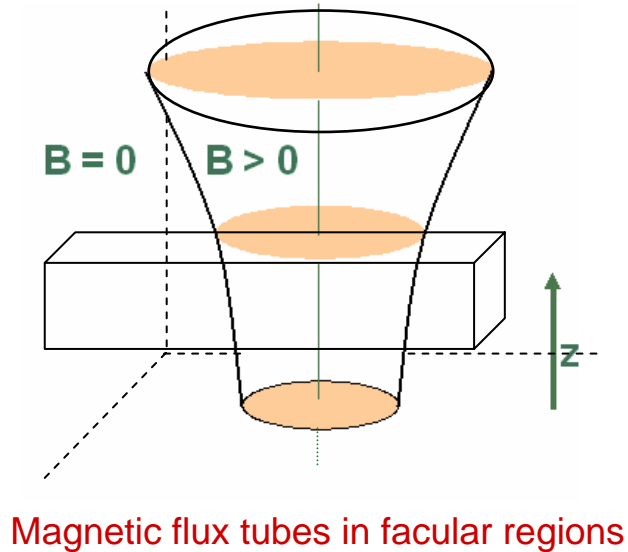


— Flux tube model



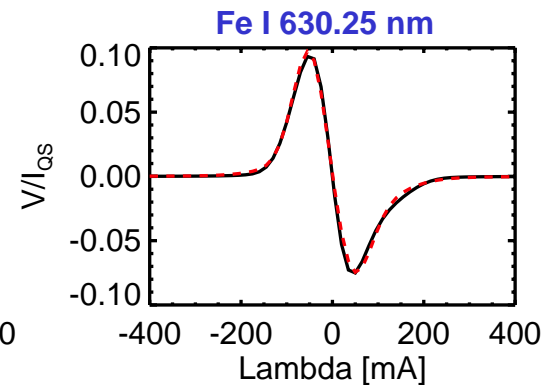
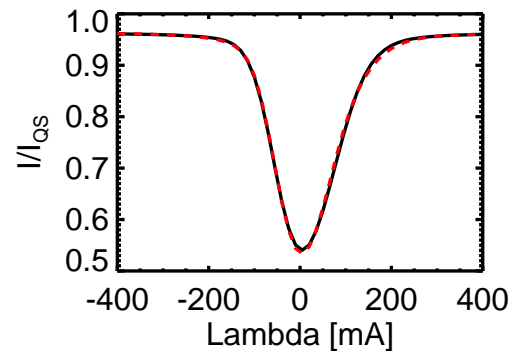
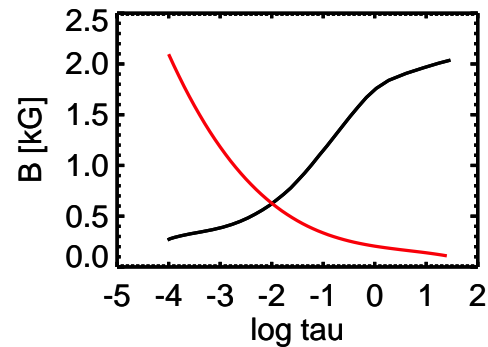
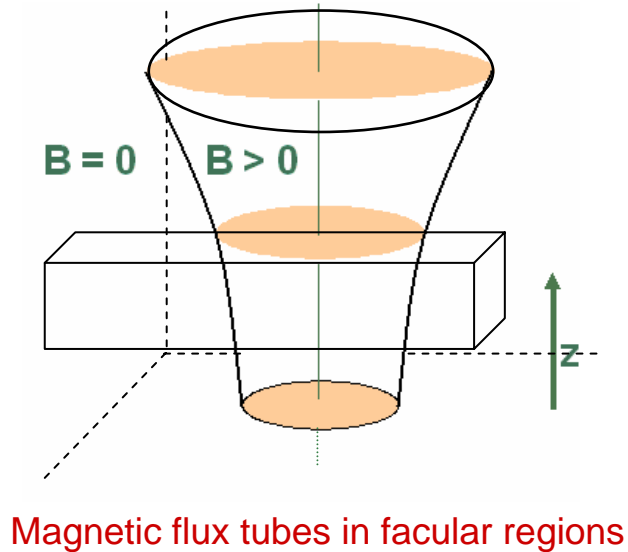
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# Available codes for inversions with gradients

<b>SIR</b>	Ruiz Cobo & del Toro Iniesta (1992)	1C & 2C atmospheres, arbitrary stratifications, any photospheric line
<b>SIR/FT</b>	Bellot Rubio et al. (1996)	Flux tube model, arbitrary stratifications, any photospheric line
<b>SIR/NLTE</b>	Socas-Navarro et al. (1998)	NLTE line transfer, arbitrary stratifications
<b>SIR/GAUS</b>	Bellot Rubio (2003)	Uncombed penumbral model, arbitrary stratifications
<b>SIR/JUMP</b>	Bellot Rubio (2007)	Canopy-like atmospheres
<b>SPINOR</b>	Frutiger & Solanki (2001)	1C & 2C atmospheres, arbitrary stratifications, any photospheric line, molecular lines, flux tube model, uncombed model
<b>LILIA</b>	Socas-Navarro (2001)	1C atmospheres, arbitrary stratifications
<b>MISMA IC</b>	Sánchez Almeida (1997)	MISMA model, arbitrary stratifications, any photospheric line



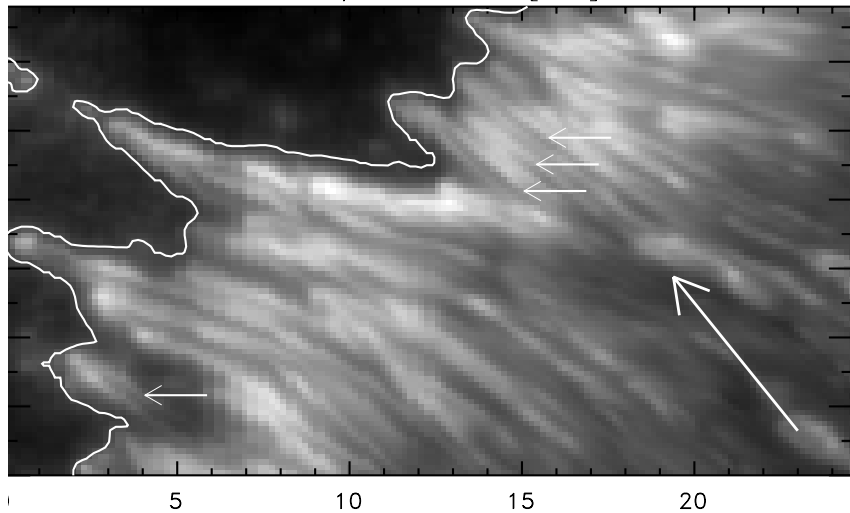
# Tips and tricks

- First of all, look at the profiles
- Try a ME inversion, it usually works
  - If the  $V$  profiles are very asymmetric, fit only  $I$ ,  $Q$ , and  $U$
- Examine the fits: are they reasonably good?

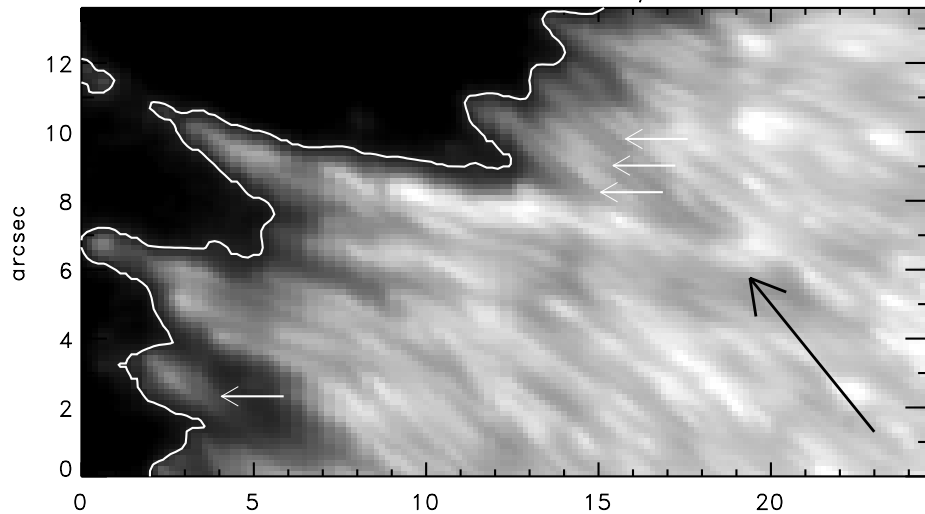


# 1C SIR inversion of Hinode/SP data

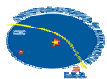
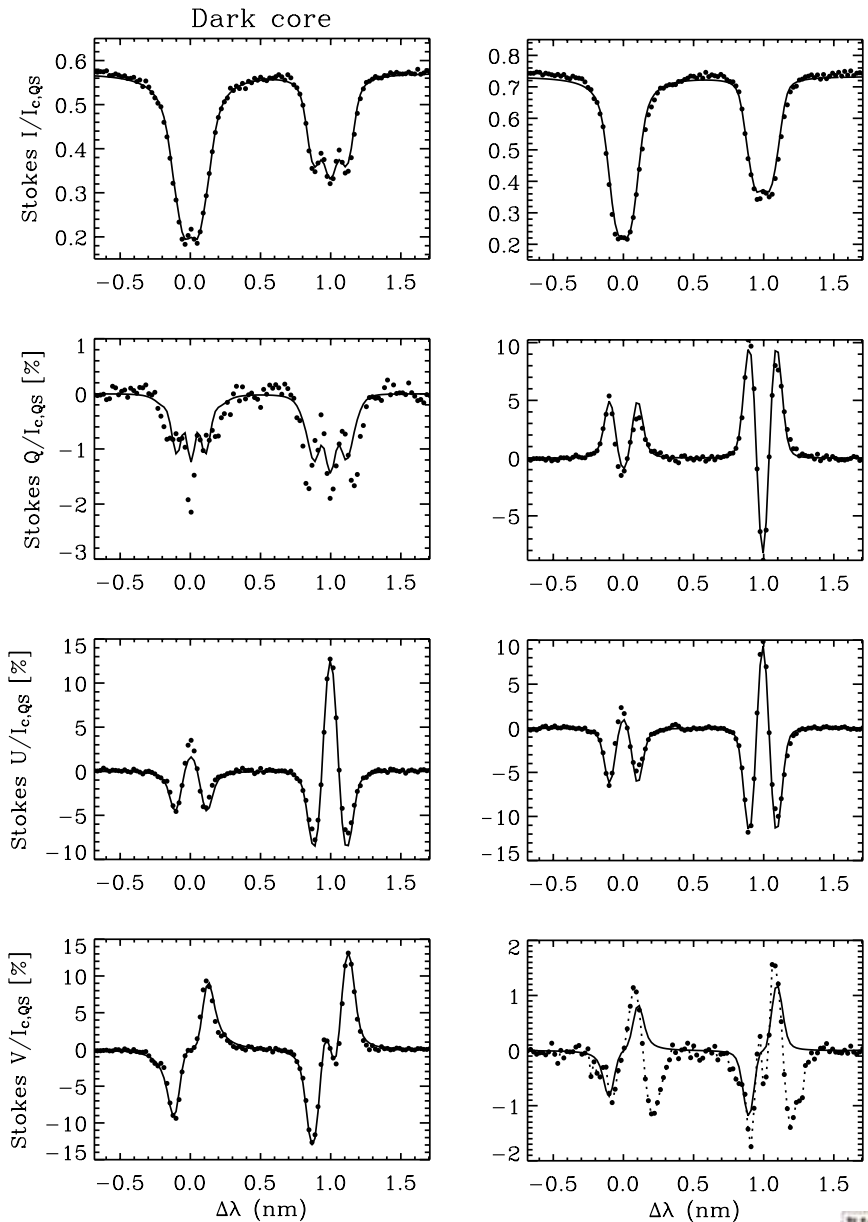
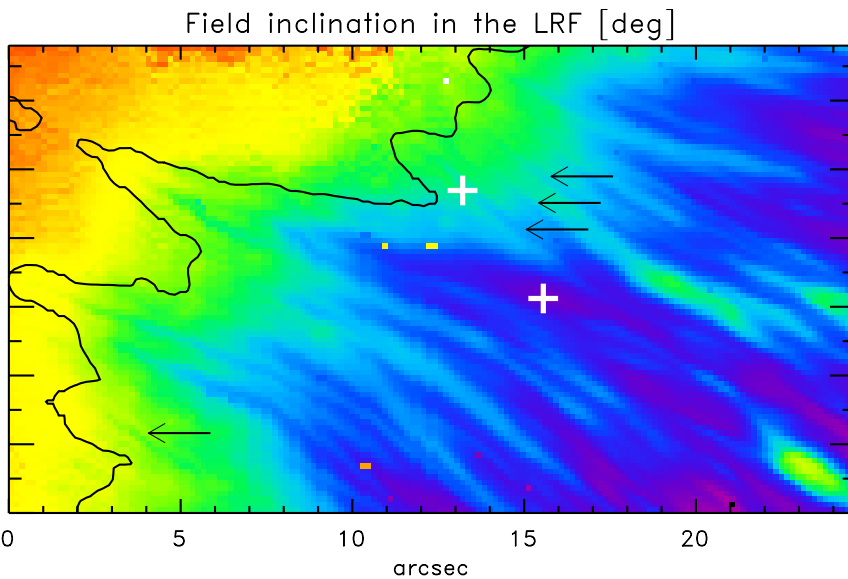
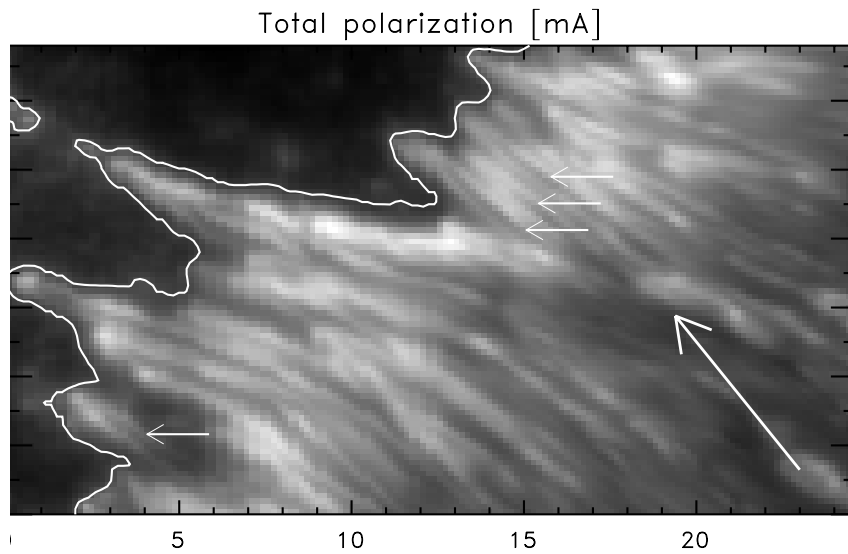
Total polarization [mA]



Continuum intensity



# 1C SIR inversion of Hinode/SP data



# Tips and tricks

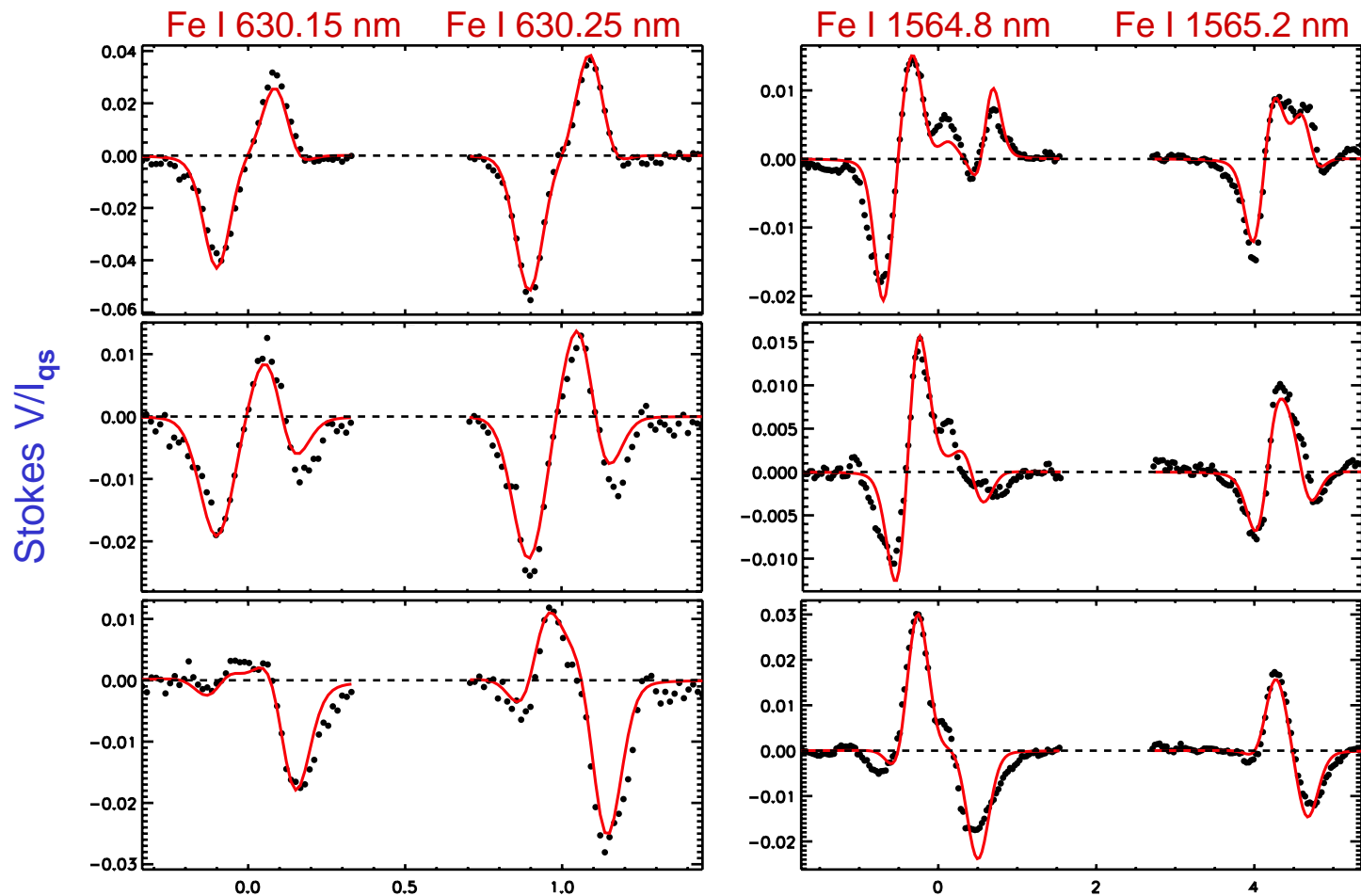
- First of all, look at the profiles
- Try a ME inversion, it usually works
  - If the V profiles are very asymmetric, fit only I, Q, and U
- Examine the fits: are they reasonably good?
- Identify
  - Pixels with bad fits and/or large asymmetries
  - Regions where interesting physical processes occur
- Run SIR inversions on these pixels
  - Which model are you going to use?  
1C model, 2C model, flux tube model, uncombed model?



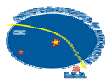


# Uncombed inversion of penumbral profiles

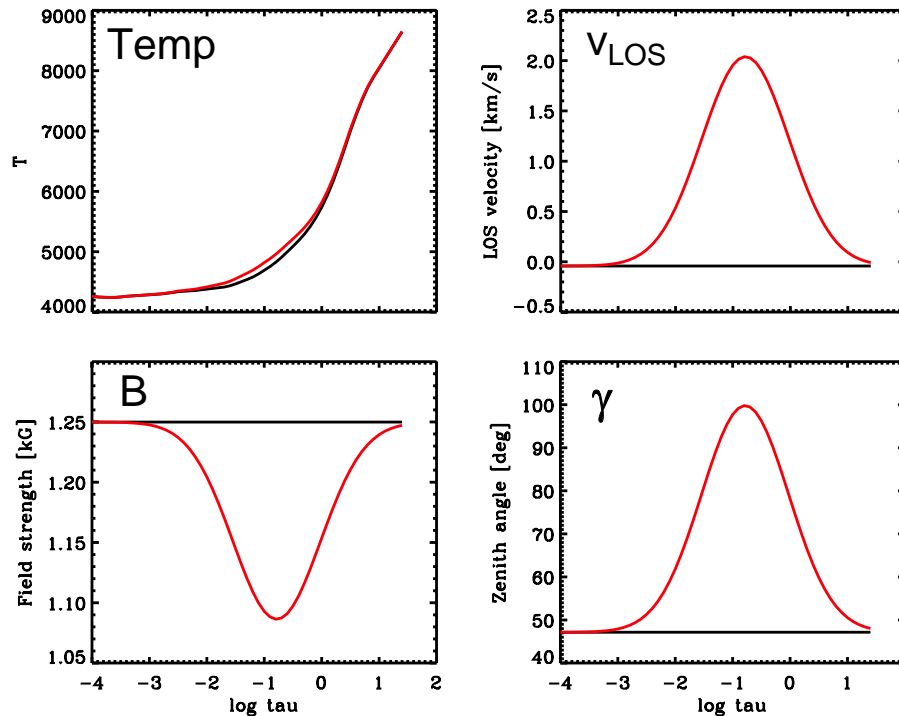
## SIR/GAUS inversion of simultaneous visible and IR observations



Beck et al. (in prep)



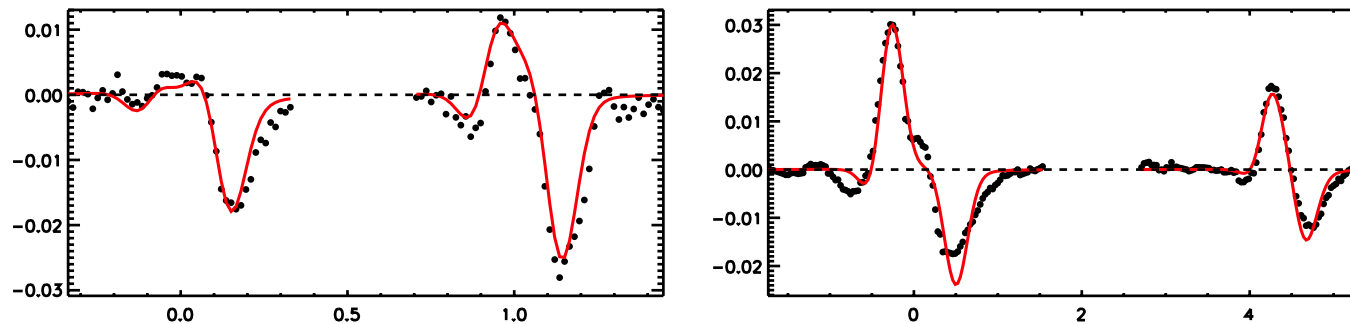
# Uncombed inversion of penumbral profiles



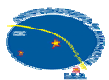
Best-fit uncombed model

Visible and IR profiles observed at 1" are compatible with **flux tubes** embedded in a more vertical and stronger background field

Stokes  $V/I_{\text{qs}}$



Beck et al. (in prep)



# Tips and tricks

- First of all, look at the profiles
- Try a ME inversion, it usually works
  - If the V profiles are very asymmetric, fit only I, Q, and U
- Examine the fits: are they reasonably good?
- Identify
  - Pixels with bad fits and/or large asymmetries
  - Regions where interesting physical processes occur
- Run SIR inversions on these pixels
  - Which model are you going to use?  
1C model, 2C model, flux tube model, uncombed model?
  - Use ME results as initialization
  - Give more weight to the strangest Stokes parameter
  - Keep it simple! See if linear stratifications (2 nodes) are sufficient
- Ask yourself if the retrieved model atmosphere makes sense!!
- You have experts in-house: ask them for advice (Jan-san)

# Running SIR: input files

```

emacs@orion.iaa.es
File Edit Options Buffers Tools Help

Number of cycles (*) : 1 ! (0=synthesis)
!
Stray light file : ! (none=no stray light contam)
PSF file : ! (none=no convolution with PSF)
Wavelength grid file (s) : malla.grid ! (none=automatic selection)
Atomic parameters file : LINES ! (none=DEFAULT LINES file)
Abundances file : THEVENIN ! (none=DEFAULT ABUNDANCES file)
Initial guess model 1 (*) : guess.mod !
Initial guess model 2 :
Weight for Stokes I : 1 ! (DEFAULT=1; 0=not inverted)
Weight for Stokes Q : 4 ! (DEFAULT=1; 0=not inverted)
Weight for Stokes U : 4 ! (DEFAULT=1; 0=not inverted)
Weight for Stokes V : 4 ! (DEFAULT=1; 0=not inverted)
AUTOMATIC SELECT. OF NODES? : 0 ! (DEFAULT=0=no; 1=yes)
Nodes for temperature 1 : 2
Nodes for electr. press. 1 :
Nodes for microturb. 1 : 1
Nodes for magnetic field 1 : 1
Nodes for LOS velocity 1 : 1
Nodes for gamma 1 : 1
Nodes for phi 1 : 1
Invert macro turbulence 1? : 1 ! (0 or blank=no, 1=yes)
Nodes for temperature 2 :
Nodes for electr. press. 2 :
Nodes for microturb. 2 :
Nodes for magnetic field 2 :
Nodes for LOS velocity 2 :
Nodes for gamma 2 :
Nodes for phi 2 :
Invert macro turbulence 2? : ! (0 or blank=no, 1=yes)
Invert filling factor? : ! (0 or blank=no, 1=yes)
Invert stray light factor? : ! (0 or blank=no, 1=yes)
mu*cos(theta) : 0.64 ! (DEFAULT: mu=1. mu<0 => West)
Estimated S/N for I : 200 ! (DEFAULT: 1000)
Continuum contrast : ! (DEFAULT: not used)
Tolerance for SVD : ! (DEFAULT value: 1e-4)
Initial diagonal element : ! (DEFAULT value: 1.e-3)
Splines/Linear Interpolation : ! (0 or blank=splines, 1=linear)
Gas pressure at surface 1 : ! (0 or blank=Pe boundary cond.)
Gas pressure at surface 2 : ! (0 or blank=Pe boundary cond.)
Magnetic pressure term? : 0 ! (0 or blank=no, 1=yes)
NLTE Departures filename : ! blank= LTE (Ej. depart_6494.dat)

*** sir.trol (Text Fill)--L1--C0--Top

```

## PROFILE FILE

```

emacs@orion.iaa.es
File Edit Options Buffers Tools Help

1.00000 -583.463 0.744716 0.000127651 -0.00144671 -0.00170201
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1.00000 -411.223 0.735525 0.000170201 0.000936167 -0.00221262
1.00000 -389.693 0.742163 0.00062906 0.00140416 0.00193907
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1.00000 -346.633 0.739014 0.00204242 0.00221262 -0.00659530
1.00000 -325.103 0.729611 0.000723356 0.00276577 0.00531679
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1.00000 -282.043 0.723824 -8.51097e-05 -0.000484803 -0.0123321
1.00000 -260.513 0.727994 -0.00127651 -0.000949694 -0.00504201
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1.00000 -195.923 0.702461 -0.00088483 -0.00297852 -0.0265511
1.00000 -174.393 0.678252 0.000538255 -0.00078596 -0.0284236
1.00000 -152.863 0.686679 -0.00276577 -0.00497839 -0.0282534
1.00000 -131.333 0.637872 -0.00527624 -0.00253557 -0.0340403
1.00000 -109.803 0.624213 0.00399973 0.00195732 0.0433545
1.00000 -88.273 0.576983 0.00472309 0.000488054 0.0545195
1.00000 -66.743 0.542261 -0.00421248 -0.00488483 -0.0738248
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1.00000 -2.153 0.35679 -0.00523342 -0.0158713 -0.161393
1.00000 19.370 0.393214 -0.0100419 -0.0198710 -0.136459
1.00000 40.907 0.259472 -0.0120843 -0.00851067 -0.0844624
1.00000 62.437 0.237303 0.0117184 0.00527624 0.0272741
1.00000 83.967 0.256661 -0.0192328 0.0169776 -0.0101695
1.00000 105.497 0.264961 -0.0185094 0.0184668 0.00574403
1.00000 127.027 0.244495 -0.0143395 0.00719101 0.0344232
1.00000 148.557 0.258706 -0.0125523 -0.00859517 0.0798521
1.00000 170.087 0.397894 0.0135736 0.0171478 0.146803
1.00000 191.617 0.375719 0.00799946 0.0212326 0.175282
1.00000 213.147 0.433499 -0.0038499 -0.0189149 0.173959
1.00000 234.677 0.519199 0.0100419 0.00578685 0.132685
1.00000 256.207 0.576302 -0.00536134 -0.00181477 0.0843773
1.00000 277.737 0.616980 -0.00808456 -0.00135151 0.0598258
1.00000 299.267 0.656424 -0.00736121 -0.00025302 0.0406930

parfil.per (Text Fill)--L1--C0--Top

```

Line index    $\Delta\lambda$  [mÅ]    $I/I_{qs}$     $Q/I_{qs}$     $U/I_{qs}$     $V/I_{qs}$

lperfiles.pro  
wperfiles.pro

# Running SIR: input files

```

emacs@orion.iaa.es
File Edit Options Buffers Tools Help

Number of cycles          (*) : 1          ! (0=synthesis)
Observed profiles        (*) : perfil.per  !
Stray light file         :               ! (none=no stray light contam)
PSF file                 :               ! (none=no convolution with PSF)
                          :               ! (none=automatic selection)
Atomic parameters file   : LINES         ! (none=DEFAULT LINES file)
Abundances file          : THEVENIN    ! (none=DEFAULT ABUNDANCES file)
Initial guess model 1    (*) : guess.mod  !
Initial guess model 2    :
Weight for Stokes I       : 1          ! (DEFAULT=1; 0=not inverted)
Weight for Stokes Q       : 4          ! (DEFAULT=1; 0=not inverted)
Weight for Stokes U       : 4          ! (DEFAULT=1; 0=not inverted)
Weight for Stokes V       : 4          ! (DEFAULT=1; 0=not inverted)
AUTOMATIC SELECT. OF NODES? : 0        ! (DEFAULT=0=no; 1=yes)
Nodes for temperature 1   : 2
Nodes for electr. press. 1 :
Nodes for microturb. 1    : 1
Nodes for magnetic field 1 : 1
Nodes for LOS velocity 1  : 1
Nodes for gamma 1        : 1
Nodes for phi 1          : 1
Invert macroturbulence 1? : 1          ! (0 or blank=no, 1=yes)
Nodes for temperature 2   :
Nodes for electr. press. 2 :
Nodes for microturb. 2    :
Nodes for magnetic field 2 :
Nodes for LOS velocity 2  :
Nodes for gamma 2        :
Nodes for phi 2          :
Invert macroturbulence 2? :                ! (0 or blank=no, 1=yes)
Invert filling factor?    :                ! (0 or blank=no, 1=yes)
Invert stray light factor? :                ! (0 or blank=no, 1=yes)
mu=cos(theta)             : 0.64       ! (DEFAULT: mu=1. mu<0 => West)
Estimated S/N for I       : 200        ! (DEFAULT: 1000)
Continuum contrast        :              ! (DEFAULT: not used)
Tolerance for SVD         :              ! (DEFAULT value: 1e-4)
Initial diagonal element  :              ! (DEFAULT value: 1.e-3)
Splines/Linear Interpolation :            ! (0 or blank=splines, 1=linear)
Gas pressure at surface 1  :              ! (0 or blank=Pe boundary cond.)
Gas pressure at surface 2  :              ! (0 or blank=Pe boundary cond.)
Magnetic pressure term?   : 0          ! (0 or blank=no, 1=yes)
NLTE Departures filename  :              ! blank= LTE (Ej. depart_6494.dat)

--** sir.trol (Text Fill)--L1--C0--Top--

```

## WAVELENGTH GRID FILE

```

emacs@dhcp-200-191.mtk.nao.ac.jp
File Edit Options Buffers Tools Help

IMPORTANT: a) All items must be separated by commas.
           b) The first six characters of the last line
              in the header (if any) must contain the symbol

Line and blends indicies : Initial lambda   Step   Final lambda
(in this order)          (mÅ)              (mÅ)      (mÅ)
1.2                      : -645.9.        21.53.   1743.93

: malla.grid (Text Fill) L7 C17 All

```



# Running SIR: input files

```

emacs@orion.iaa.es
File Edit Options Buffers Tools Help

Number of cycles          (*) : 1          ! (0=synthesis)
Observed profiles        (*) : perfil.per  !
Stray light file         :                ! (none=no stray light contam)
PSF file                 :                ! (none=no convolution with PSF)
Wavelength grid file     (s) : malla.grid  ! (none=automatic selection)
                          :                ! (none=DEFAULT LINES file)
Abundances file          : IHEVEN.IN      ! (none=DEFAULT ABUNDANCES file)
Initial guess model 1    (*) : guess.mod  !
Initial guess model 2    :
Weight for Stokes I       : 1          ! (DEFAULT=1; 0=not inverted)
Weight for Stokes Q       : 4          ! (DEFAULT=1; 0=not inverted)
Weight for Stokes U       : 4          ! (DEFAULT=1; 0=not inverted)
Weight for Stokes V       : 4          ! (DEFAULT=1; 0=not inverted)
AUTOMATIC SELECT. OF NODES? : 0        ! (DEFAULT=0=no; 1=yes)
Nodes for temperature 1   : 2
Nodes for electr. press. 1 :
Nodes for microturb. 1    : 1
Nodes for magnetic field 1 : 1
Nodes for LOS velocity 1  : 1
Nodes for gamma 1        : 1
Nodes for phi 1          : 1
Invert macro turbulence 1? : 1          ! (0 or blank=no, 1=yes)
Nodes for temperature 2   :
Nodes for electr. press. 2 :
Nodes for microturb. 2    :
Nodes for magnetic field 2 :
Nodes for LOS velocity 2  :
Nodes for gamma 2        :
Nodes for phi 2          :
Invert macro turbulence 2? :                ! (0 or blank=no, 1=yes)
Invert filling factor?    :                ! (0 or blank=no, 1=yes)
Invert stray light factor? :                ! (0 or blank=no, 1=yes)
mu=cos(theta)             : 0.64       ! (DEFAULT: mu=1. mu<0 => West)
Estimated S/N for I       : 200        ! (DEFAULT: 1000)
Continuum contrast        :                ! (DEFAULT: not used)
Tolerance for SVD         :                ! (DEFAULT value: 1e-4)
Initial diagonal element  :                ! (DEFAULT value: 1.e-3)
Splines/Linear Interpolation :                ! (0 or blank=splines, 1=linear)
Gas pressure at surface 1  :                ! (0 or blank=Pe boundary cond.)
Gas pressure at surface 2  :                ! (0 or blank=Pe boundary cond.)
Magnetic pressure term?    : 0          ! (0 or blank=no, 1=yes)
NLTE Departures filename  :                ! blank= LTE (Ej. depart_6494.dat)

--:** sir.trol (Text Fill)--L1--C0--Top--

```

## ATOMIC PARAMETER FILE

```

emacs@orion.iaa.es
File Edit Options Buffers Tools Help

1-Ht 1 6301.5012 1.0 3.654 -0.5 5P 2.0- 5U 2.0 0.243 2.3520e-14
2-Ht 1 6302.4936 1.0 3.686 -1.236 5P 1.0- 5U 0.0 0.240 2.3976e-14

: LINES (Text Fill) L3 C0 All

```

Line  
index    Atom    $\lambda$     E    $\chi$    log gf   transition

# Running SIR: input files

```

emacs@orion.iaa.es
File Edit Options Buffers Tools Help

Number of cycles      (*) : 1      ! (0=synthesis)
Observed profiles    (*) : perfil.per !
Stray light file      :          ! (none=no stray light contam)
PSF file             :          ! (none=no convolution with PSF)
Wavelength grid file (s) : malla.grid ! (none=automatic selection)
Atomic parameters file : LINES    ! (none=DEFAULT LINES file)
Abundances file       : THEVENIN   ! (none=DEFAULT ABUNDANCES file)

Initial guess model 2 :
Weight for Stokes I   : 1
Weight for Stokes Q   : 4
Weight for Stokes U   : 4
Weight for Stokes V   : 4
AUTOMATIC SELECT. OF NODES? : 0
Nodes for temperature 1 : 2
Nodes for electr. press. 1 :
Nodes for microturb. 1 : 1
Nodes for magnetic field 1 : 1

--:** sir.trol (Text Fill)--

```

MODEL FILE

```

emacs@orion.iaa.es
File Edit Options Buffers Tools Help

1.191199 1.000000 0.000000E+00
1.4000 8886.7 3.07074E+03 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -1.1482E+02 2.1731E+05 3.7768E-07
1.3000 8728.1 2.52511E+03 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -1.0502E+02 2.1085E+05 3.7393E-07
1.2000 8569.4 2.06383E+03 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -9.5670E+01 2.0474E+05 3.7053E-07
1.1000 8410.7 1.67605E+03 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -8.6739E+01 1.9896E+05 3.6747E-07
1.0000 8252.1 1.35199E+03 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -7.8201E+01 1.9347E+05 3.6474E-07
0.9000 8093.4 1.06291E+03 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -7.0025E+01 1.8826E+05 3.6231E-07
0.8000 7914.7 8.37268E+02 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -6.2107E+01 1.8324E+05 3.6103E-07
0.7000 7696.1 6.04266E+02 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -5.4178E+01 1.7821E+05 3.6153E-07
0.6000 7447.4 4.05270E+02 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -4.5889E+01 1.7294E+05 3.6293E-07
0.5000 7178.0 2.61987E+02 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -3.6876E+01 1.6719E+05 3.6429E-07
0.4000 6880.1 1.56440E+02 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -2.6596E+01 1.6061E+05 3.6536E-07
0.3000 6592.3 9.00154E+01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 -1.4459E+01 1.5286E+05 3.6304E-07
0.2000 6322.8 5.28586E+01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 0.0000E+00 1.4374E+05 3.5603E-07
0.1000 6084.1 3.25596E+01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 1.7050E+01 1.3330E+05 3.4316E-07
0.0000 5875.4 2.1316E+01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 3.6610E+01 1.2186E+05 3.2486E-07
-0.1000 5696.8 1.45885E+01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 5.8242E+01 1.0997E+05 3.0238E-07
-0.2000 5543.1 1.11864E+01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 8.1274E+01 9.8263E+04 2.7768E-07
-0.3000 5409.4 8.73575E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 1.0504E+02 8.7213E+04 2.5255E-07
-0.4000 5295.8 7.06379E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 1.2903E+02 7.7100E+04 2.2806E-07
-0.5000 5192.1 5.80998E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 1.5291E+02 6.8018E+04 2.0521E-07
-0.6000 5093.5 4.81886E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 1.7653E+02 5.9945E+04 1.8436E-07
-0.7000 4994.8 4.06224E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 1.9975E+02 5.2811E+04 1.6563E-07
-0.8000 4906.1 3.34879E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 2.2255E+02 4.6524E+04 1.4855E-07
-0.9000 4827.5 2.82042E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 2.4496E+02 4.0987E+04 1.3300E-07
-1.0000 4758.8 2.35137E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 2.6702E+02 3.6110E+04 1.1887E-07
-1.1000 4690.1 2.02242E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 2.8878E+02 3.1812E+04 1.0625E-07
-1.2000 4631.5 1.72307E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 3.1028E+02 2.8020E+04 9.4772E-08
-1.3000 4582.8 1.46063E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 3.3157E+02 2.4673E+04 8.4341E-08
-1.4000 4539.1 1.27741E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 3.5269E+02 2.1721E+04 7.4964E-08
-1.5000 4495.5 1.10053E+00 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 3.7366E+02 1.9116E+04 6.6613E-08
-1.6000 4456.8 9.52386E-01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 3.9451E+02 1.6816E+04 5.9107E-08
-1.7000 4428.2 8.33382E-01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 4.1526E+02 1.4788E+04 5.2313E-08
-1.8000 4409.5 7.37876E-01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 4.3592E+02 1.3002E+04 4.6192E-08
-1.9000 4390.8 6.53162E-01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 4.5649E+02 1.1432E+04 4.0787E-08
-2.0000 4372.2 5.76038E-01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 4.7698E+02 1.0052E+04 3.6016E-08
-2.1000 4353.5 5.11436E-01 2.256E+02 2.3692E+03 4.6400E+05 1.4605E+02 1.2604E+02 4.9737E+02 8.8384E+03 3.1803E-08

--:** guess_1_mod (Text Fill)--L1-C0-Top
Loading muwheel...done

```

leemod.pro  
 escribemod.pro  
 modelador2.x  
 equilibrium.x  
 geometrical.x

$\log \tau$   $T$   $P_e$   $V_{mic}$   $B$   $V_{LOS}$   $\gamma$   $\phi$   $z$  [km]  $P_g$   $\rho$

# Running SIR/GAUSS: input files

```

X muj.trol - emacs@hsc24.mtk.nao.ac.jp
File Edit Options Buffers Tools Help

Number of cycles      (*) : 2          ! (0=synthesis)
Observed profiles    (*) : profile.per ! (cosi)
Stray light file      :              ! (none=no stray light contam)
PSF file             : ins_prof.psf   ! (none=no convolution with PSF)
Wavelength grid file (s) : wavelength.grid ! (cosi)
Atomic parameters file : lines.l      ! (none=DEFAULT LINES file)
Abundances file       : thevenin.t    ! (none=DEFAULT ABUNDANCES file)
Initial guess model 1 (*) : avpenleq3.mod
Initial guess model 2 (*) :
File containing gaussian : muj.gaus    ! (DEFAULT: none)
Weight for Stokes I   : 1             ! (DEFAULT=1; 0=not inverted)
Weight for Stokes Q   : 1             ! (DEFAULT=1; 0=not inverted)
Weight for Stokes U   : 1             ! (DEFAULT=1; 0=not inverted)
Weight for Stokes V   : 4,4          ! (DEFAULT=1; 0=not inverted)
AUTOMATIC SELECT. OF NODES? :          ! (DEFAULT=0=no; 1=yes)
Nodes for temperature 1 : 1,2
Nodes for electr. press. 1 :
Nodes for microturb. 1 : 0
Nodes for magnetic field 1 : 1
Nodes for LOS velocity 1 : 1
Nodes for gamma 1 : 0,1
Nodes for phi 1 : 1
Invert macro turbulence 1? : 0          ! (0 or blank=no, 1=yes)
Nodes for temperature 2 : 1
Nodes for electr. press. 2 : 0
Nodes for microturb. 2 : 0
Nodes for magnetic field 2 : 0,1
Nodes for LOS velocity 2 : 0,1
Nodes for gamma 2 : 1
Nodes for phi 2 : 1
Invert macro turbulence 2? :          ! (0 or blank=no, 1=yes)
Invert filling factor? : 0             ! (0 or blank=no, 1=yes)
Invert stray light factor? : 0         ! (0 or blank=no, 1=yes)
Nodes for center of gaussian : 0,1     ! Only 1 allowed if gaussian
Nodes for width of gaussian : 1        ! only 0 or 1 allowed if gaussian
mu=cos (theta) : 0.84                ! (DEFAULT: mu=1. mu<0 => West)
Estimated S/N for I : 800             ! (DEFAULT: 1000)
Continuum contrast :                  ! (DEFAULT: not used)
Tolerance for SVD :                  ! (DEFAULT value: 1e-4)
Initial diagonal element :            ! (DEFAULT value: 1.e1)
Gas pressure at surface 1 : 5.e3       ! (0 or blank=Pe boundary cond.
Gas pressure at surface 2 : 5.e3       ! (0 or blank=Pe boundary cond.
Magnetic pressure term? : 0            ! (0 or blank=no, 1=yes)

-- muj.trol (Fundamental) --L10--All--

```

## GAUSSIAN FILE

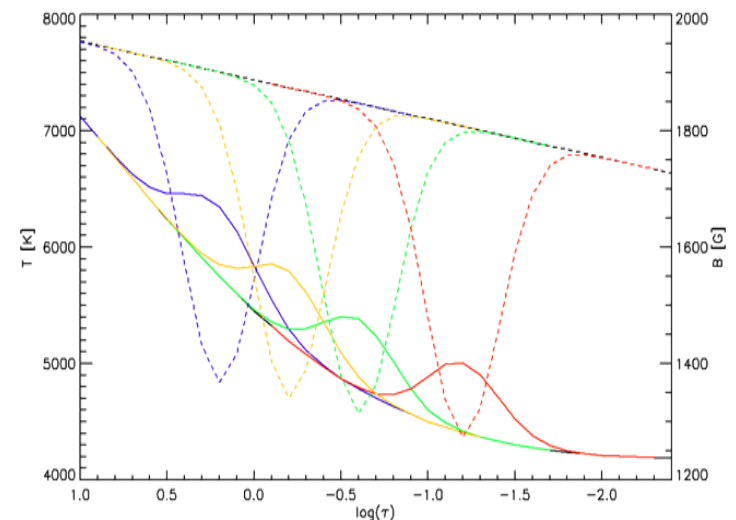
```

X muj.gaus - emacs@hsc24.mtk.nao.ac.jp
File Edit Options Buffers Tools Help

Central position index : 0.2
Sigma (optical depth) : 0.5
Amplitude for T : 800.
Amplitude for vmic : -1.0E+05
Amplitude for B : -500.
Amplitude for v : -1.0E+05
Amplitude for gamma : -30.0
Amplitude for fi : -5.

-- muj.gaus (Fundamental) --L1--All--

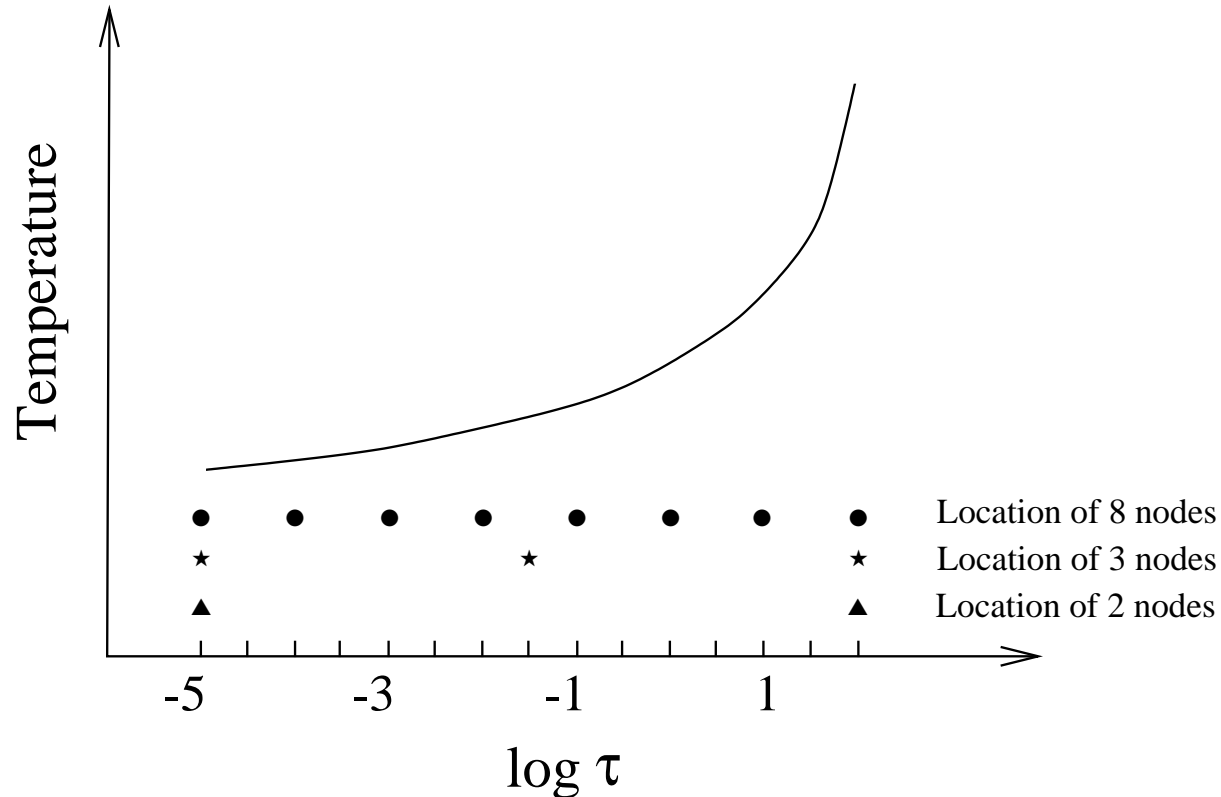
```





# Concept of nodes

- Keeping the number of free parameters small:
  - Atmospheric parameters perturbed in coarse grid (nodes)
  - Full stratifications in finer grid by cubic spline interpolation

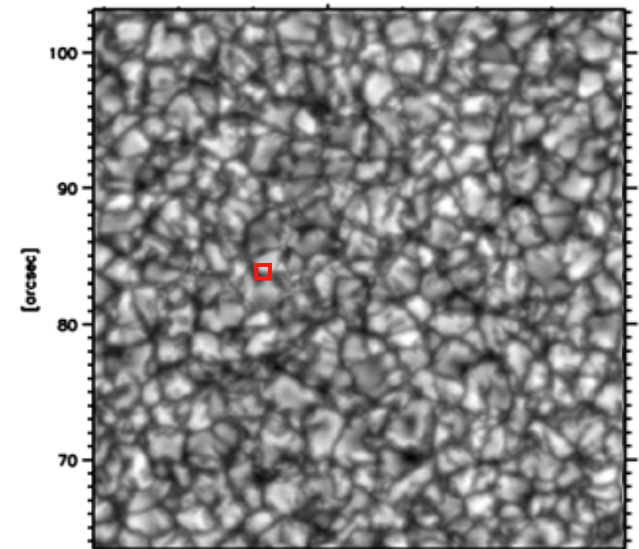
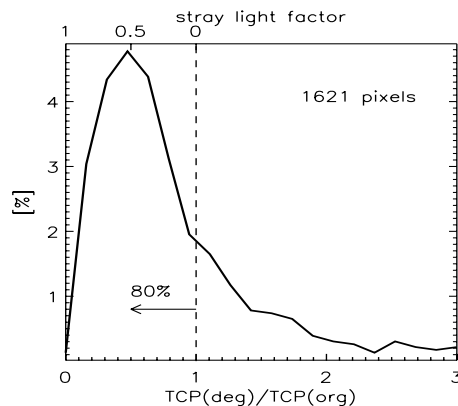
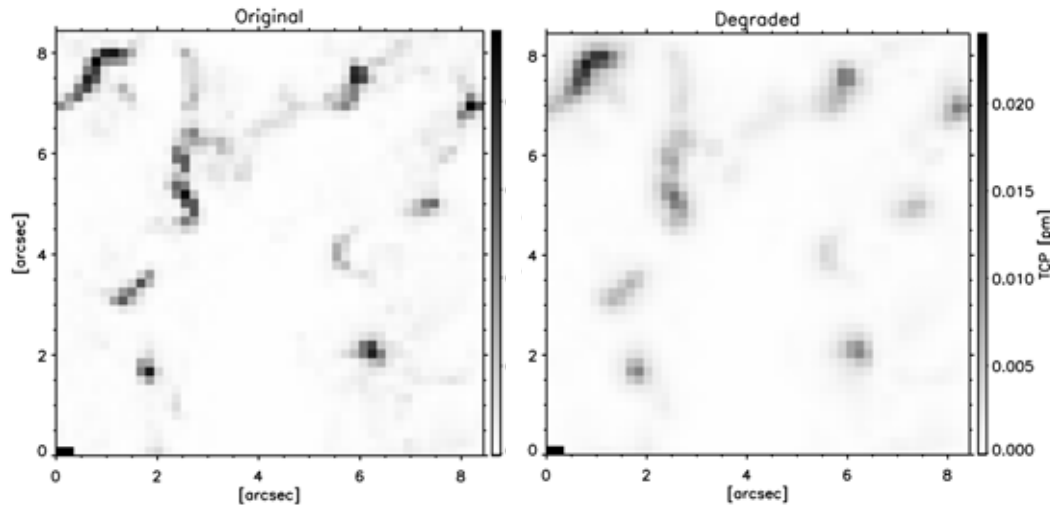


# Stray-light considerations

- Stray-light in ME inversions:
  - Equivalent to a magnetic filling factor  $f = 1 - \alpha$
- Stray-light in SIR inversions:
  - It is NOT equivalent to a magnetic filling factor
  - In fact, SIR has two free parameters:  $\alpha$  and  $f$
- Global vs local stray-light profile
  - Classical treatment: global stray-light profile (over FOV)
  - Orozco Suárez et al. (2007): local stray-light profile accounts for telescope diffraction

# Local stray light

- Telescope diffraction reduces the polarization signal
- Important for weak fields and noisy signals!

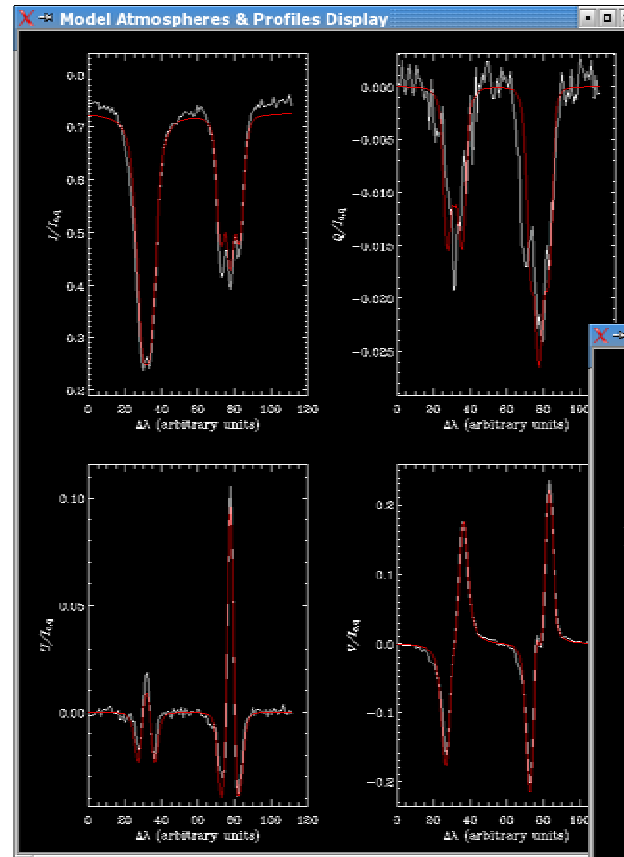
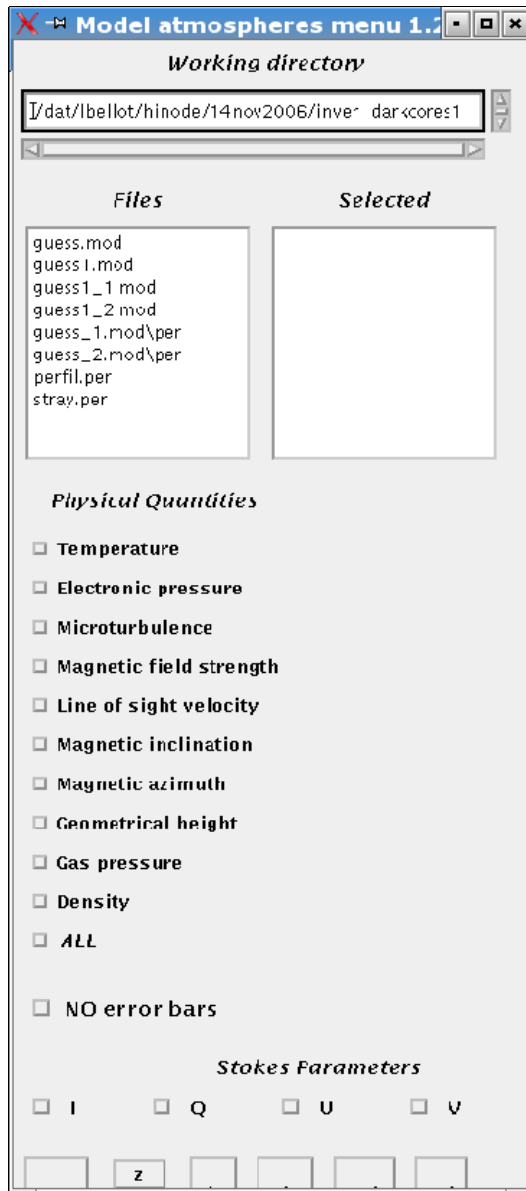


Unpolarized stray light  
Average over a box 1"-  
wide centered on the  
pixel of interest

# Executing the inversion

`echo sir.trol | sir.x`

# Visualizing SIR results: graphics.pro



Stokes profiles

Model atmospheres

